

Template attacks on implementations of cryptographic algorithms

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Research topics:

- Electronics design IP protection,
- Hardware security,
- Physical attacks:
 - Active: fault attacks.
 - Passive: side-channel analysis/attacks

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Symmetric cryptography

Cryptography aims at delivering several properties, such as:

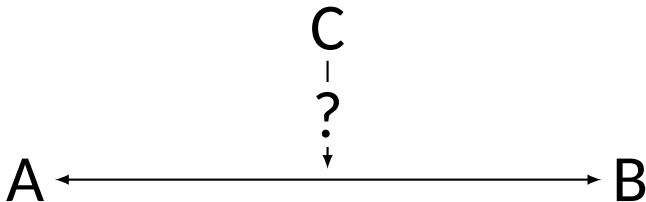
- › integrity,
- › authenticity,
- › **confidentiality**

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Confidentiality:

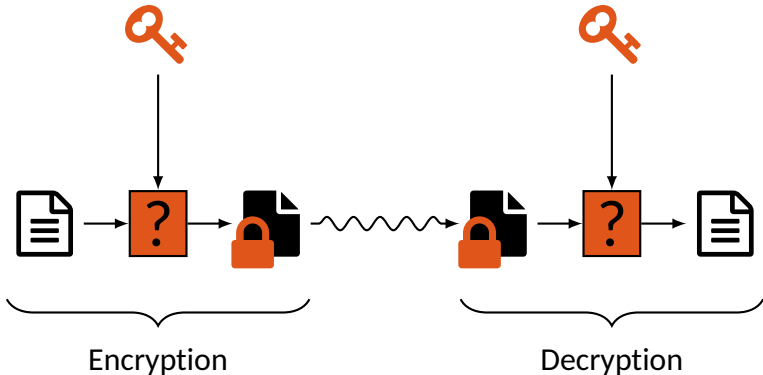
Parties A and B can communicate without party C understanding.



The message is **encrypted** by A and **decrypted** by B.

The **same key** is used for encryption and decryption.

By obtaining the key, we break the confidentiality.



The Rijndael block cipher [1] was standardized by NIST in 2001. It is now referred to as AES (Advanced Encryption Standard).

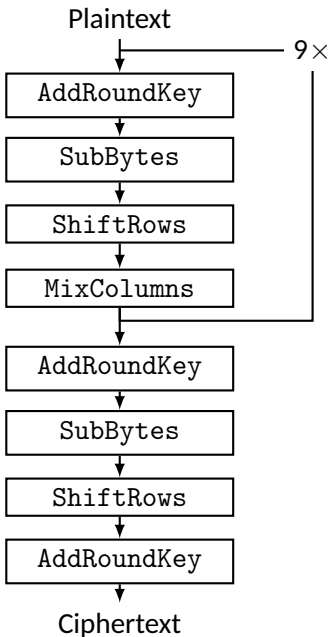
A **block** cipher operates on **blocks** of data.

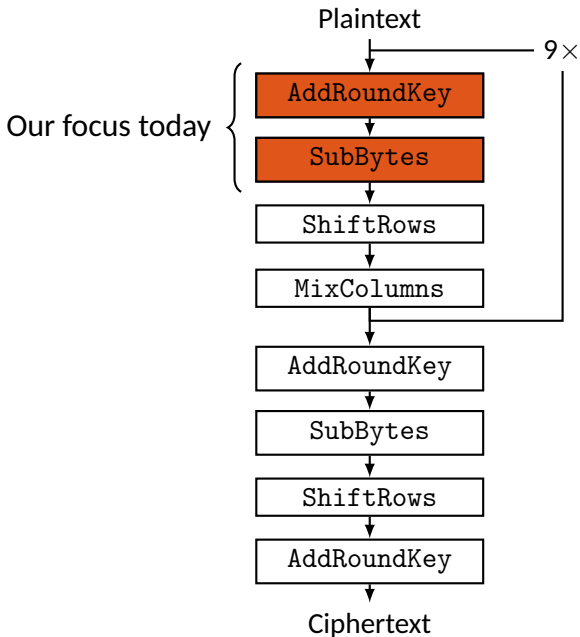
AES-128 [2] operates with:

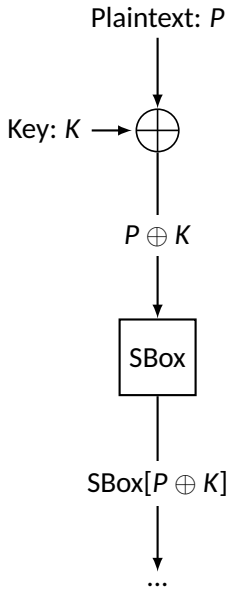
- a 128-bit key,
- on 128-bit blocks.

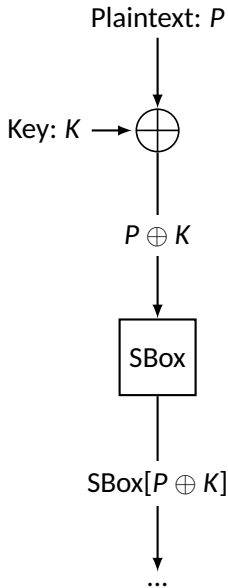
[1] J. Daemen and V. Rijmen. "Rijndael for AES". *The Third Advanced Encryption Standard Candidate Conference*. New York, USA: National Institute of Standards and Technology, Apr. 2000, pp. 343–348.

[2] AES-192 and AES-256 exist too but are not covered here









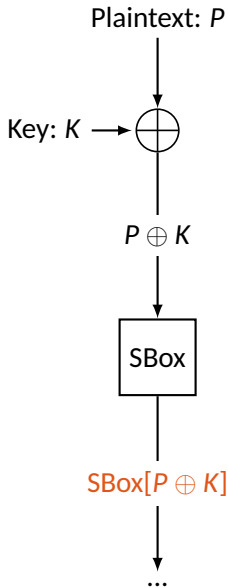
SBox is an $\{0, 1\}^8 \rightarrow \{0, 1\}^8$ substitution table.

AES S-box

| | 00 | 01 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 0a | 0b | 0c | 0d | 0e | 0f |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 00 | 63 | 7c | 77 | 7b | f2 | 6b | 6f | c5 | 30 | 01 | 67 | 2b | fe | d7 | ab | 76 |
| 10 | ca | 82 | c9 | 7d | fa | 59 | 47 | f0 | ad | d4 | a2 | af | 9c | a4 | 72 | c0 |
| 20 | b7 | fd | 93 | 26 | 36 | 3f | f7 | cc | 34 | a5 | e5 | f1 | 71 | d8 | 31 | 15 |
| 30 | 04 | c7 | 23 | c3 | 18 | 96 | 05 | 9a | 07 | 12 | 80 | e2 | eb | 27 | b2 | 75 |
| 40 | 09 | 83 | 2c | 1a | 1b | 6e | 5a | a0 | 52 | 3b | d6 | b3 | 29 | e3 | 2f | 84 |
| 50 | 53 | d1 | 00 | ed | 20 | fc | b1 | 5b | 6a | cb | be | 39 | 4a | 4c | 58 | cf |
| 60 | d0 | ef | aa | fb | 43 | 4d | 33 | 85 | 45 | f9 | 02 | 7f | 50 | 3c | 9f | a8 |
| 70 | 51 | a3 | 40 | 8f | 92 | 9d | 38 | f5 | bc | b6 | da | 21 | 10 | ff | f3 | d2 |
| 80 | cd | 0c | 13 | ec | 5f | 97 | 44 | 17 | c4 | a7 | 7e | 3d | 64 | 5d | 19 | 73 |
| 90 | 60 | 81 | 4f | dc | 22 | 2a | 90 | 88 | 46 | ee | b8 | 14 | de | 5e | 0b | db |
| a0 | e0 | 32 | 3a | 0a | 49 | 06 | 24 | 5c | c2 | d3 | ac | 62 | 91 | 95 | e4 | 79 |
| b0 | e7 | c8 | 37 | 6d | 8d | d5 | 4e | a9 | 6c | 56 | f4 | ea | 65 | 7a | ae | 08 |
| c0 | ba | 78 | 25 | 2e | 1c | a6 | b4 | c6 | e8 | dd | 74 | 1f | 4b | bd | 8b | 8a |
| d0 | 70 | 3e | b5 | 66 | 48 | 03 | f6 | 0e | 61 | 35 | 57 | b9 | 86 | c1 | 1d | 9e |
| e0 | e1 | f8 | 98 | 11 | 69 | d9 | 8e | 94 | 9b | 1e | 87 | e9 | ce | 55 | 28 | df |
| f0 | 8c | a1 | 89 | 0d | bf | e6 | 42 | 68 | 41 | 99 | 2d | 0f | b0 | 54 | bb | 16 |

The column is determined by the least significant nibble, and the row by the most significant nibble. For example, the value $9a_{16}$ is converted into $b8_{16}$.

https://en.wikipedia.org/wiki/Rijndael_S-box



SBox mapping is **known** and **reversible**.
We assume the **plaintext is known too**.

We want **the key!**

AES is byte-oriented: the state is a 4×4 matrix of **bytes**.

| | | | |
|-------|-------|----------|----------|
| s_0 | s_4 | s_8 | s_{12} |
| s_1 | s_5 | s_9 | s_{13} |
| s_2 | s_6 | s_{10} | s_{14} |
| s_3 | s_7 | s_{11} | s_{15} |

Our target intermediate value is in fact split into **16 bytes**

| | | | |
|------------------------|------------------------|------------------------------|------------------------------|
| $SBox[p_0 \oplus k_0]$ | $SBox[p_4 \oplus k_4]$ | $SBox[p_8 \oplus k_8]$ | $SBox[p_{12} \oplus k_{12}]$ |
| $SBox[p_1 \oplus k_1]$ | $SBox[p_5 \oplus k_5]$ | $SBox[p_9 \oplus k_9]$ | $SBox[p_{13} \oplus k_{13}]$ |
| $SBox[p_2 \oplus k_2]$ | $SBox[p_6 \oplus k_6]$ | $SBox[p_{10} \oplus k_{10}]$ | $SBox[p_{14} \oplus k_{14}]$ |
| $SBox[p_3 \oplus k_3]$ | $SBox[p_7 \oplus k_7]$ | $SBox[p_{11} \oplus k_{11}]$ | $SBox[p_{15} \oplus k_{15}]$ |





We will **divide and conquer** and recover the 128-bit key **byte by byte**.

Side-channel attacks

Side-channel attacks principle

Physical quantities measured on the device depend on the data the device handles.

Examples of physical quantities:

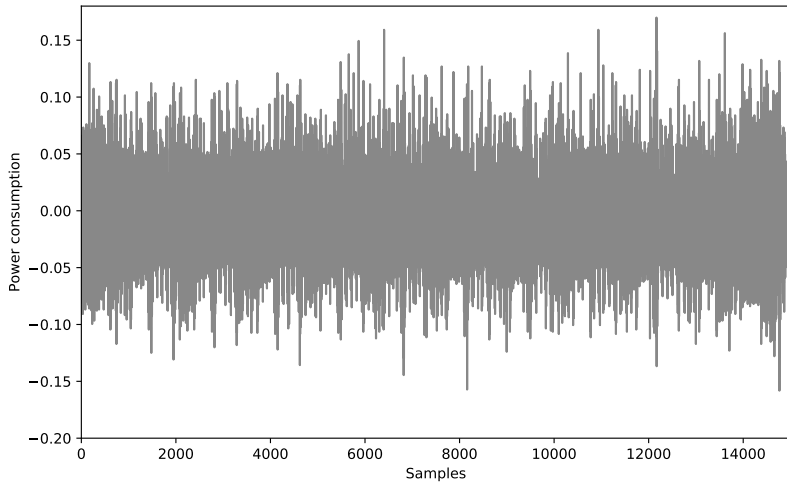
-  power consumption,
-  electromagnetic radiations,
-  sound,
-  photonic emissions.

A **microcontroller** runs multiple AES encryptions.

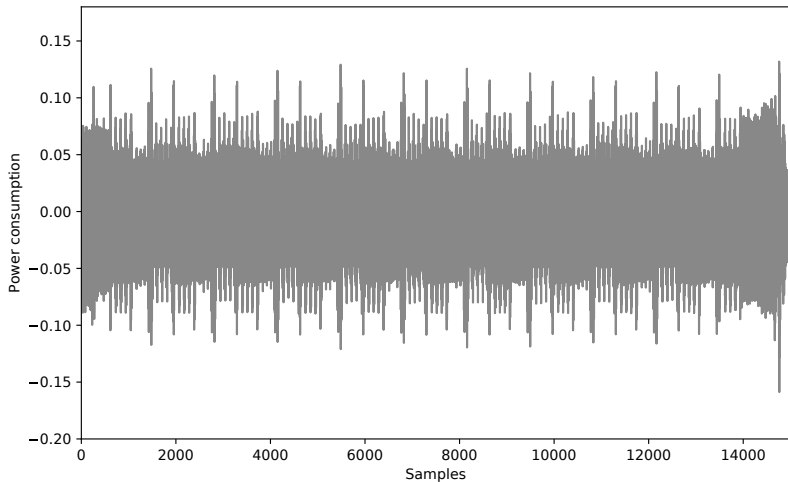
We put an **electromagnetic probe** above it and **record** the electromagnetic field.



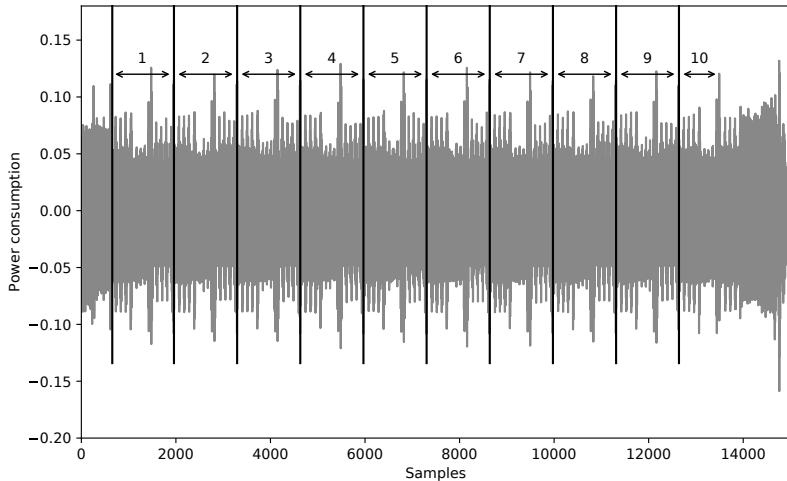
First, **one measurement**



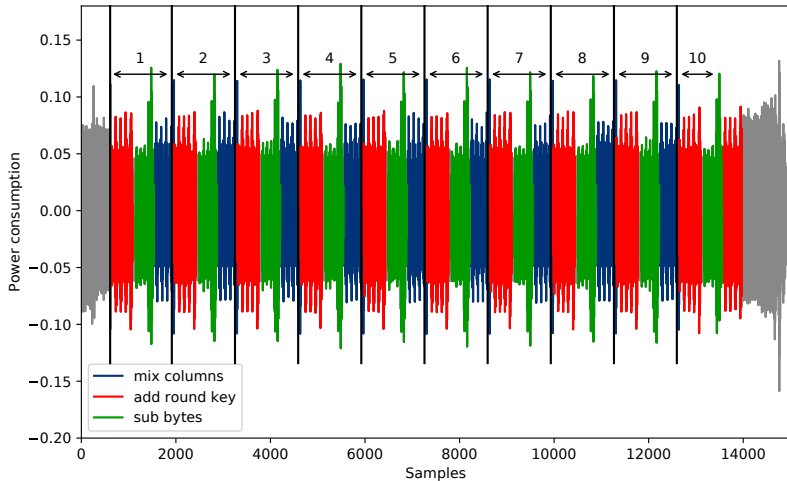
Averaging 50 identical measurements (denoising)



AES rounds are visible



AES **transformations** are visible within rounds



Theory of template attacks

Template attacks were introduced in 2002 [3].

The **information leakage** can be modeled as a **Gaussian** distribution. This is **fully described** by the following parameters:

- the mean: μ
- the variance: σ^2

A **template** is the (μ, σ^2) pair.

A template attack follows a two-step process:

- **profiling** phase,
- **matching** phase.

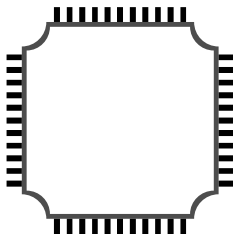
[3] S. Chari, J. R. Rao, and P. Rohatgi. "Template Attacks". *CHES*. 2002, pp. 13–28.

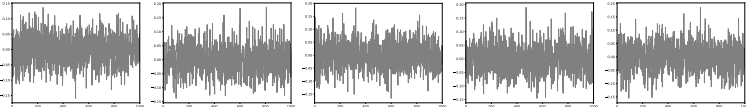
Aim:

build a **template** (μ, σ^2) for every intermediate value $\in \{0, \dots, 255\}$.

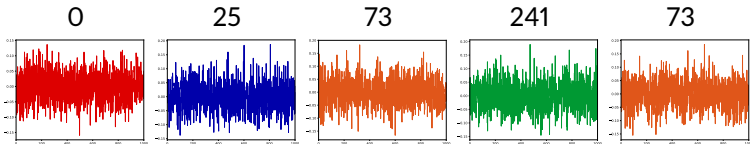
We do this on an **open** device:

- ▶ we **control the inputs**: **key** K and **plaintext** P .
- ▶ we know the **intermediate value** of interest: $SBox[p_i \oplus k_i]$
- ▶ we can **perform side-channel measurements** on it.





Intermediate value $SBox[p_i \oplus k_i] =$



We build 256 sets of traces, according to the **intermediate value**.

\mathcal{T}_i is the set for which the intermediate value is equal to i .

First, we find a **point of interest** :

- we compute the **average signal** for each set,
- we compute **pairwise differences** between average signals,
- we keep the point where this is **maximum**.

Then, for each set, at this point of interest, we compute :

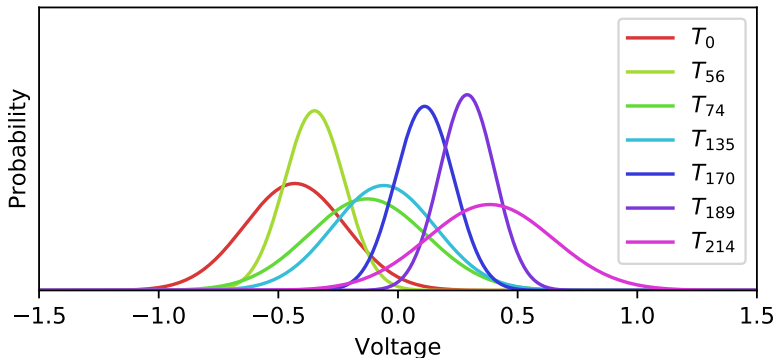
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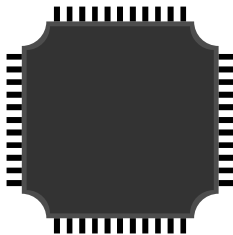
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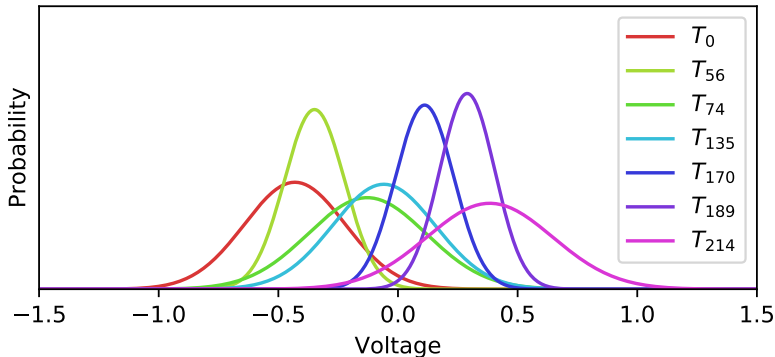


Attack on a **closed** device:

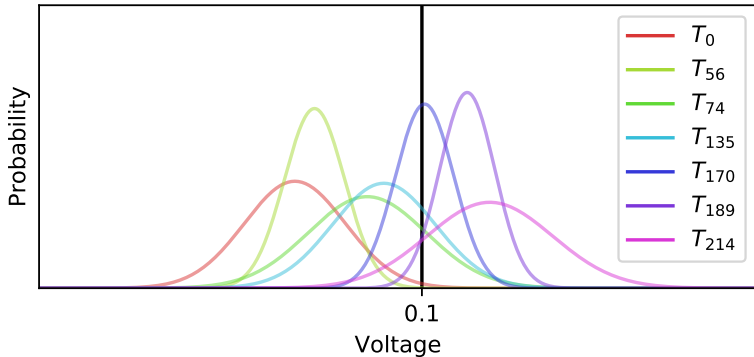
- ▶ we know the **plaintext** input P but **not the key**,
- ▶ we look for the intermediate value of interest: $SBox[p_i \oplus k_i]$,
- ▶ we can perform **side-channel measurements** on it.



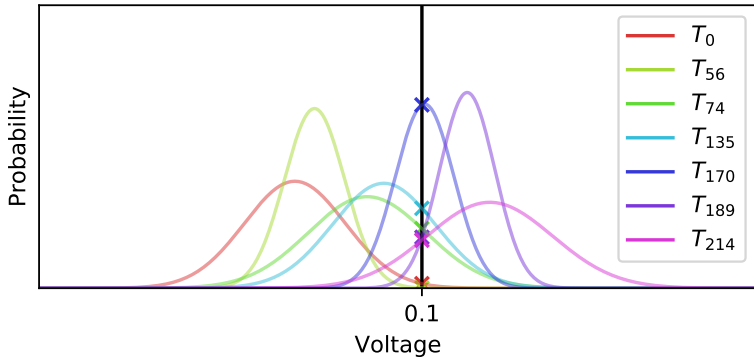
Let us assume we measure a voltage of 0.1.
We now “match” this on our templates.



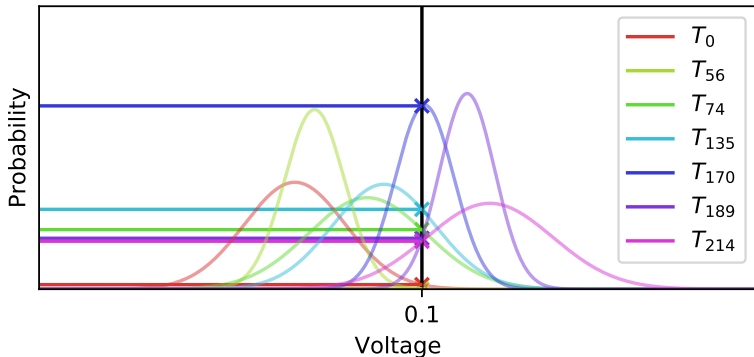
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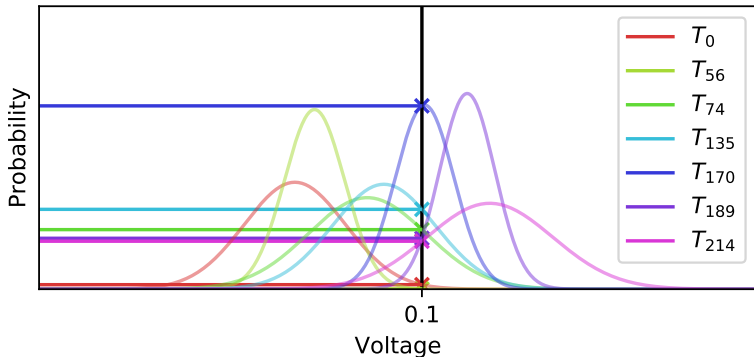


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Values can then be **enumerated** until we find **the correct key**.

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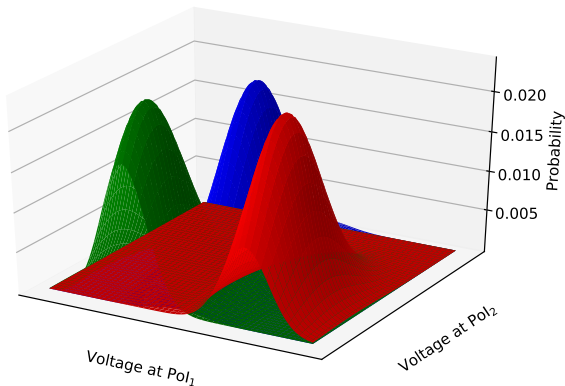
Improvements and options

One measurement is (usually) not enough for the matching phase.
We **combine** information obtained from multiple measurements.

| Intermediate values | Measurements | | | | Overall Probability |
|------------------------|--------------|-------------|-----|-------------|------------------------|
| | 1 | 2 | ... | N | |
| 0 | 0.12 | 0.15 | | 0.13 | $\prod_{i=0}^N p_i$ |
| 1 | 0.01 | 0.02 | | 0.01 | |
| 2 | 0.13 | 0.14 | | 0.16 | |
| 3 | 0.02 | 0.03 | | 0.04 | |
| ... | ... | ... | | ... | |
| 255 | 0.04 | 0.05 | | 0.03 | |

We can stop when the **confidence** is large enough.

With only **one** point of interest, we may miss valuable information.
We can take into account **more points of interest**.
Templates are then **multivariate** Gaussian distributions.

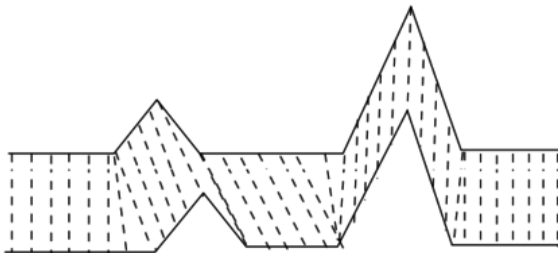


These are specified by a **mean vector** and a **covariance matrix**.

For the template attack to work, samples must be **perfectly aligned**.

Pre-processing them might be necessary:

- ▶ Variable shift based on correlation value (linear),
- ▶ Dynamic time warping (non-linear).

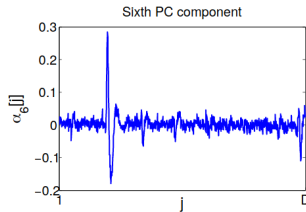
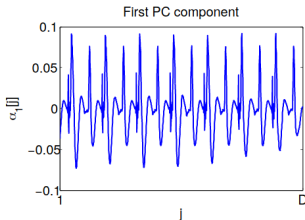


Selecting points of interest is **not easy**...

Information can spread over **multiple samples**.

Principal Component Analysis can help reduce the data dimension.

Get **principal components** of the signal, but which one to keep? [4]



[5]

Still an open question, relies on attacker's knowledge.

[4] L. Batina, J. Hogenboom, and J. G. J. van Woudenberg. "Getting More from PCA: First Results of Using Principal Component Analysis for Extensive Power Analysis". *CT-RSA*. 2012, pp. 383–397.

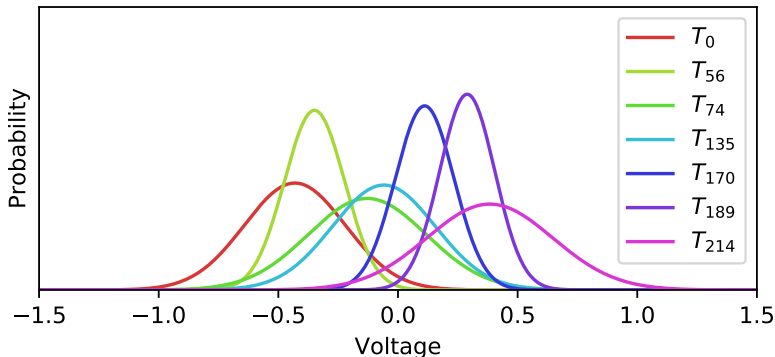
[5] E. Cagli, C. Dumas, and E. Prouff. "Enhancing Dimensionality Reduction Methods for Side-Channel Attacks". *CARDIS*. 2015, pp. 15–33.

As highlighted in [6], computational problems may arise in practice:

- The covariance matrix might **not** be **invertible**,
- Multiplying the probabilities can lead to **floating-point errors**.

They propose the following solutions:

- Use the **logarithm** of the multivariate normal distribution,
- Use a **pooled** covariance matrix,

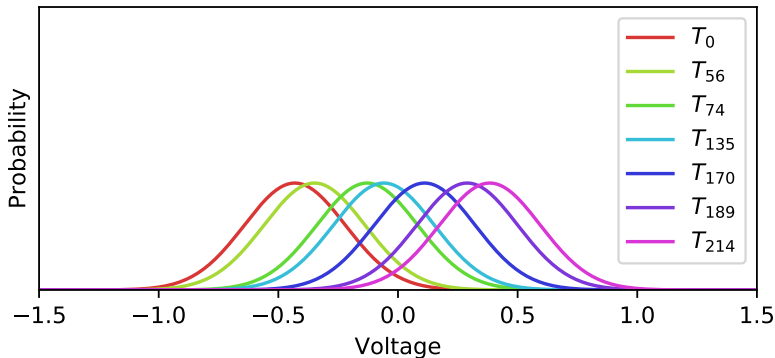


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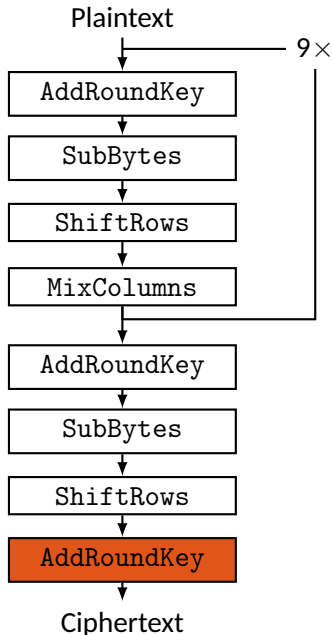
The presented attack requires to know the **plaintext**.

Same principles apply if we know the **ciphertext** instead.

This time we attack the **last** round.

We recover $C \oplus K_{10}$ and we know C .

From the **round-key** K_{10} we recover the key K by **reverting the key-schedule**.



Experimental aspects

Q: How many traces are needed for the **profiling** phase?

[7] N. Veyrat-Charvillon, B. Gérard, M. Renauld, and F. Standaert. “An Optimal Key Enumeration Algorithm and Its Application to Side-Channel Attacks”. *SAC*. vol. 7707. 2012, pp. 390–406.

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- Q: Other questions?

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Conclusion

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Even **protected** implementations can be targeted.

They can be used to attack other algorithms (asymmetric, etc.)

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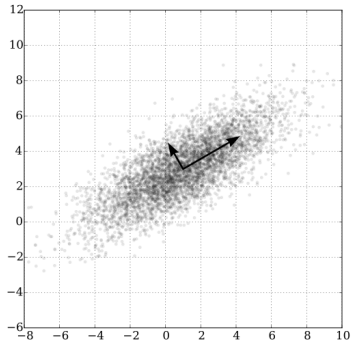
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— Questions? —

Backup slides



Identify the components where data varies the most.
Orthogonal vectors.